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A. 研究概要

部分因子環の Jones 指数の取りうる値については, 1980 年代から多くの研究があり, 一般の部分因子環の場合については, 4 以下で $4 \cos^2 \pi/n$, $n = 3, 4, 5, \dots$ の形の値を取り, 4 以上の値はすべて取りうるということがわかっている. 共形場理論を作用素環の立場から研究するときの対象は, 局所共形ネットという作用素環の族であるが, 部分因子環のなす局所共形ネットについて, Jones 指数の取りうる値を決める問題を Carpi, Longo と共に考えた. 任意の自然数の値が実現可能であることは簡単にわかるが, それ以外の値については, 一般の部分因子環の場合より, ずっと強い制限が付き, 最小の値は, $4 \cos(\pi/10)$, 次の値は $3 + \sqrt{3}$ であることを示した. これに関連して, $A-D-E$ 型部分因子環について, Dynkin 図形の偶頂点に対応する対象たちがどのような braiding を持ちうるかを完全に決定した. 境界共形場理論, 超共形場理論の作用素環の研究も続行した.

The possible values of the Jones indices of subfactors have been studied since 1980's and they are now completely determined. That is, the possible values are of the form $4 \cos^2 \pi/n$, $n = 3, 4, 5, \dots$, when they are below 4, and all the values larger than or equal to 4 are also realized. In the operator algebraic approach to conformal field theory, we study local conformal nets, which are certain families of von Neumann algebras, and we have studied the problem to determine the possible values of the Jones indices of local conformal nets of subfactors with Carpi and Longo. It is easy to see that all positive integer values are realized. Besides these values, we have shown that the two smallest values are $4 \cos(\pi/10)$ and $3 + \sqrt{3}$. In connection to this result, we have also classified possible braiding structures on the objects corresponding to the even vertices of the Dynkin diagrams for the $A-D-E$ subfactors.

We have also continued our operator algebraic studies on boundary conformal field theory and superconformal field theory.

B. 発表論文

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C. 口頭発表

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 3. Quantum field theory and operator algebra, 5th Asian Mathematical Conference, Kuala Lumpur (Malaysia), June 2009.
 4. Subfactors and representation theory for von Neumann algebras, 12th Workshop: Non-commutative harmonic analysis, Bedlewo (Poland), August 2009.
 5. Superconformal field theory, Moonshine and operator algebras 12th Workshop: Non-commutative harmonic analysis, Bedlewo (Poland), August 2009.
 6. Superconformal field theory and noncommutative geometry, Subfactor Seminar, UC Berkeley (U.S.A.), September 2009.
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- D. 講義
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- E. 修士・博士論文
1. (修士)Noppakhun SUTHICHITRANONT: Grothendieck rings for non-modular and non-symmetric pre-modular categories of rank 4
 2. (修士) 酒匂宏樹 (SAKO Hiroki): Stone-Cech boundaries of discrete groups and measure equivalence theory
- F. 对外研究サービス
1. *Communications in Mathematical Physics* の editor.
 2. *International Journal of Mathematics* の chief editor.
 3. *Japanese Journal of Mathematics* の managing editor.
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