

教授 (Professor)

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#### A. 研究概要

2023 年以降の 3 年間の研究活動は専攻長および副研究科長の業務で限定されたものになったが、2021 年以降の 5 年間においては、主に以下の 3 テーマで総計約 900 ページの論文を著した。

##### 1. 緩増加等質空間

リー群  $G$  が作用する空間  $X$  に対して、正則表現  $L^2(X)$  がいつ緩増加になるかという問題を提起した (Y. Benoist と共同). まず,  $X$  が簡約型の場合に力学系の手法を用いて  $L^2(X)$  の行列要素の  $L^p$  評価を与え [J. Euro. Math], 次に, 一般の  $X$  に対して, 群作用をもつ測度空間のなす空間に新しい半順序を導入するアイデアを使って, 緩増加性の幾何的判定法を証明した (第 2 論文 [Chicago Univ. Press, 2022]). 第 3 論文 [J. Lie Theory, 2022] で非緩増加な実簡約型等質空間の完全な分類を与え, 第 4 論文 [J. Inst. Jussieu, 2023] では, 緩増加性, リー代数の極限に関する位相的性質, 余随伴軌道の幾何, 凸多面体の組合せ論の間の関係性を発見し, 証明した. さらにテンソル積表現への応用を [J. Alg., 2023] で著した.

##### 2. 対称性破れ作用素の構成と分類問題

簡約リー群の無限次元表現の「分岐則」に関して, 定性的理論から定量的理論に深化させるプログラムを提起し推進した ([8]).

**2.A.** (定性的理論) 離散的な分岐則の理論の要となる  $K'$ -admissibility の十分条件 ([Ann. Math., 1998] の主定理の 1 つ) が, 実は必要十分条件であることをシンプレクティック幾何の手法を用いて証明を与えた [Kostant 追悼論文, 2021].

**2.B.** (定性的理論 2) 分岐則の重複度が有限・一様有界になるための判定条件を無限次元表現の“サイズ”を定式化して与え, 特に,  $H$ -distinguished な  $G$  の表現が部分群  $G'$  に関して有界重複度をもつ 3 つ組  $(H, G, G')$  を可視的作用の理論を援用して分類した ([JLT, 2023] 他).

**2.C.** (定性的理論 3) 有界重複度をもつ群の組に対し **fence** という概念を導入し, 分岐則の重複度が fence を越えない場合に一定であるという定理を証明し [1,4], 志村多様体などへの応用を見出し始めた [2,4,8].

**2.D.** (定量的理論 —ホログラフィック変換) 対称性破れ作用素の族の双対として“ホログラフィック変換”の概念を導入し [Ann. Inst. Fourier, 2020], 擬リーマン空間形の離散系列表現の分岐則における離散スペクトラムをホログラフィック変換で構成し, 決定した [Adv. Math., 2021].

**2.E.** (微分対称性破れ作用素の母関数) 標題の新しい概念の研究を開始した (文献 [3, 12, 13, 14]).

##### 3. 不連続群

筆者の長年のモチーフである「リーマン幾何学の枠組を越えた不連続群」に関する研究において, スペクトル理論の構築に踏み込んだ. 幾何学的な準備として, 離散群の作用の不連続性を量的に評価する sharpness という概念を導入し, 高次元タイヒミュラー空間上で安定な離散スペクトラムを構成した [Adv. Math.]. さらに, 隠れた対称性を表す微分作用素環の構造定理を与え, それを土台として無限次元表現の分岐則理論を援用し, 標準的な擬リーマン局所対称空間に対するスペクトル分解定理の証明を完成させ [書籍 1], 高次元・高階の空間における不連続群がどこまで変形できるかについて甘中氏と研究し長編の論文を著した [6].

For the past five years, since 2021, I have been working on the following research topics.

##### 1. Tempered homogeneous spaces

As a contribution to global analysis on homogeneous spaces beyond symmetric spaces, I collaborated with Y. Benoist on 4 papers [J. Euro. Math. '15]-[J. Inst. Jussieu, 2023], and established a geometric criterion for temperedness of the regular representation on  $L^2(G/H)$ . A complete classification of nontempered reductive homogeneous spaces  $G/H$  was accomplished, and further connections with other disciplines of mathematics were explored.

##### 2. Restriction of representations: symmetry breaking operators

Branching problems concern the restriction of irreducible representations to subgroups. I proposed a general program in [Progr. Math., 2015] to advance the theory of branching problems for reductive groups.

**2.A** Regarding the discrete decomposability

of restricted representations, I proved— using symplectic geometry—the converse of one of the main theorems from my earlier microlocal analysis work [Ann. Math., 1998] in [Kostant Memorial, 2021].

**2.B** I formulated and proved criteria for finite multiplicity and bounded multiplicity property in the restriction of “small” infinite-dimensional representations to reductive subgroups in [Adv. Math. 2021, JLT2023]. In particular, I established a classification of triples  $H \subset G \supset G'$  such that every irreducible  $H$ -distinguished representation of  $G$  has bounded multiplicity upon restriction to symmetric pair  $(G, G')$ ,

**2.C** Joint with B. Speh, I classified *symmetry breaking operators* (SBOs) of principal series for a pair of Lorentz groups (Memoirs of AMS, 2015; Lect. Notes Math., 2018), providing the first complete classification of SBOs. Moreover, we introduced a notion of **fence** to analyze the behavior of multiplicity under translation functors [1, 2, 4, 8].

**2.D,E** As a kind of “inverse” to symmetry breaking, I introduced the concept of **holomorphic transform** in [Adv. Math. 2021] and further developed it in a joint paper with Pevzner ([Ann. Inst. Fourier 2020]). We also developed the theory of **generating operators for SBOs** in [3, 12, 13, 14].

### 3. Analysis on locally symmetric spaces— beyond the Riemannian case

Building on my long-standing interest in discontinuous groups beyond the Riemannian case, I initiated the study of global analysis on locally non-Riemannian symmetric spaces with F. Kassel in [Adv. Math] and proved the existence of “stable spectrum” under small deformations of discontinuous groups. Furthermore, building on the structure theorem of three algebras of invariant differential operators, established a spectral theory on standard quotients  $\Gamma \backslash G/H$  in [Book 2025]. Moreover, together with Kannaka, I advanced deformation theory of discontinuous groups, with emphasis

on Zariski-dense deformation [6, 10].

### B. 発表論文

(論文は 2025 年以降のものを記載する。2024 年以前の論文は、過去の Annual Report の各年度に記載。)

1. T. Kobayashi, Stability of branching multiplicities for orthogonal Gelfand pairs. Preprint. 50 pages, 2026.
2. T. Kobayashi, Stability of Multiplicities in Symmetry Breaking: The  $\mathfrak{sl}_2$  Case, to appear. 30 pages, 2026.
3. T. Kobayashi and M. Pevzner, Rankin–Cohen brackets in Representation Theory, preprint. 39 pages. arXiv.org/abs/2601.15750
4. M. Harris, T. Kobayashi, and B. Speh, Translation functors, branching problems, and applications to the restriction of coherent cohomology of Shimura varieties, preprint. 100 pages. arXiv.org/abs/2509.17007
5. T. Kobayashi, Preface. In: Mikio Sato Collected Papers. Volumes I–III, Springer Nature. in Press.
6. K. Kannaka and T. Kobayashi, Zariski-dense deformations of standard discontinuous groups for pseudo-Riemannian homogeneous spaces, Preprint. 107 pages. arXiv: 2507.03476.
7. T. Kobayashi, Proper actions and representation theory. In: Representations and Characters: Revisiting the Works of Harish-Chandra and André Weil, World Scientific, Lecture Note Series **45**, Institute for Mathematical Sciences, National University of Singapore. pp. 285–343 (2026), Available also at arXiv: 2506.15616.
8. T. Kobayashi and B. Speh, How does the restriction of representations change under translations?: A story for the general linear groups and the unitary groups, preprint. 50 pages. arXiv: 2502.08479. To appear in Proc. Indian Acad. Sci. Math. Sci. a com-

- memorative volume for Harish-Chandra.
9. T. Kobayashi, Harish-Chandra's admissibility theorem and beyond, preprint. 33 pages. arXiv: 2412.20387. To appear in Proc. Indian Acad. Sci. Math. Sci. a commemorative volume for Harish-Chandra.
  10. K. Kannaka and T. Kobayashi. Deformations of standard locally homogeneous space. Proc. Japan Acad. Ser. A. Math. Sci., **102**(2), pp. 7–12, 2026.
  11. T. Kobayashi. Tempered homogeneous spaces. In A. Sasaki and K. Arashi, editors, Proceedings of the Symposium on Representation Theory 2025, pages 1–38, 2025.
  12. T. Kobayashi and M. Pevzner. A generating operator for Rankin–Cohen brackets. Journal of Functional Analysis, **289**(4):110944, 2025. 22 pages.
  13. T. Kobayashi and M. Pevzner. A short proof for Rankin–Cohen brackets and generating operators. In V. Dobrev, editor, Lie Theory and Its Applications in Physics. LT 2023, **473** of Springer Proceedings in Mathematics & Statistics, pages 3–15. Springer, 2025.
  14. T. Kobayashi, Generating operators of symmetry breaking-from discrete to continuous, Indagationes Mathematicae, **36**, (2025), pp. 631–643.
  15. T. Kobayashi, Stability region of branching multiplicities, Preprint, 2026.

著書:

1. F. Kassel and T. Kobayashi. Spectral Analysis on Standard Locally Homogeneous Spaces, Lecture Notes in Mathematics, **2367**, xi+116 pages. 2025. Springer. <https://doi.org/10.1007/978-981-96-1957-3>
2. 小林俊行, 地力をつける 微分と積分, 岩波書店, 2024 年. 278 pages. ISBN 9784000058896
3. (編集) Mikio Sato Collected Papers. Vol-

umes I–III, Editor in Chief, Springer Nature. In Press.

C. 口頭発表

1. (有限次元表現の不変量) (**1.A** から **1.C** は講演タイトル, 内容は個々に異なるが, 大きなテーマとしては繋がっているので 1 つにまとめる.) **1.A.** On a Numerical Invariant Associated with Finite-dimensional Representations of Lie Algebras and Global Geometry of Homogeneous Spaces. (opening lecture). Workshop on Representation Theory and Geometry in Ryukoku. Ryukoku University, Kyoto, Japan, 19–20 Feb 2026. **1.B.** A Numerical Invariant Associated with Finite-Dimensional Representations of Lie Algebras. Workshop on Representation Theory. Tottori, Japan, 10–12 Jan 2026. **1.C.** A Numerical Invariant Associated with Finite-Dimensional Representations of Lie Algebras. (opening lecture) Frontiers of Lie Theory: Computational Aspects and Applications (organized by Willem Adriaan De Graaf, Alessio Marrani, Piotr Jastrzębski, Aleksy Tralle). Będlewo, Poland, 28 Sep–4 Oct 2025.
2. (分岐則における translation と fence の概念の導入) (**2.A** から **2.F** は講演タイトル, 内容は個々に異なるが, 大きなテーマとしては繋がっているので 1 つにまとめる.) **2.A.** Symmetry Breaking under Translation. (Opening Lecture). Representation Theory XIX. Dubrovnik, Croatia, 22–28 June 2025. **2.B.** Symmetry Breaking under Translation. Plenary Lecture (Opening Lecture). XVI. International Workshop: Lie Theory and its Applications in Physics. Varna, Bulgaria, 16–22 June 2025. **2.C.** Symmetry Breaking under Translations. AIM-IHP seminar. Institut Henri Poincaré, France, 11 February 2025. **2.D.** Restricting representations of real reductive groups to reductive subgroups, Séminaire Groupes Ré-

- ductifs et Formes Automorphes, France, 17 March 2025. **2.E.** Symmetry Breaking under Translations. AIM-IHP seminar. Institut Henri Poincaré, France, 11 February 2025. **2.F.** Symmetry Breaking and Translation Functor. NCTS Workshop on Representation Theory and Lie Groups. Taiwan, 11–14 December 2024.
3. (不連続群のスペクトル解析と無限次元表現論をつなげる概説講演) (**3.A** と **3.B** は講演タイトルは異なるが, 大きなテーマとしては繋がっているので 1 つにまとめる.) **3.A.** Non-commutative Harmonic Analysis, Branching Problems, and Discontinuous Groups. The 7th Tunisian-Japanese Conference: Geometric and Harmonic Analysis on Homogeneous Spaces and Applications in Honor of Professor Toshiyuki Kobayashi. Monastir, Tunisia, 31 October–4 November 2023. **3.B.** On the Crossroads of Global Analysis and Representation Theory. Geometry, Analysis, and Representation Theory of Lie Groups. In Honour of Professor Toshiyuki Kobayashi (organized by Y. Oshima, H. Sekiguchi, T. Kubo, T. Okuda, Y. Tanaka, and M. Kitagawa). The University of Tokyo, 5–9 September 2022.
  4. (対称性破れ作用素の母作用素の理論) (**4.A.–4.C.** は内容は異なるが, 大きなテーマとしては繋がっているので 1 つにまとめる.) **4.A.** 29th Nordic Congress of Mathematicians with EMS. Aalborg, Denmark, 3–7 July 2023. **4.B.** (Plenary Lecture) International Workshop Lie Theory and Its Applications in Physics (LT-15). Varna, Bulgaria, 19–25 June 2023. **4.C.** Holographic Transform, 20 August, 2021, Workshop on "Actions of Reductive Groups and Global Analysis (Online Tambara), August 17–21, 2021.
  5. (可視的作用と無重複性理論・極小表現をモチーフとする大域解析) (**5.A** と **5.B** は内容は異なるが, ここでは 1 つにまとめる.) **5.A.** “Visible actions” and “only one” — Geometric structure that produces multiplicity-free representations. 東京大学大学院数理科学研究科設立 30 周年記念講演 (The 30th Anniversary Ceremony of the Foundation of the Graduate School of Mathematical Sciences). The University of Tokyo, 15 October 2022. **5.B.** 極小表現をモチーフとする大域解析 Schrödinger model of minimal representations and branching problems. Minimal Representations and Theta Correspondence: (Gordan Savin 教授還暦記念研究集会). (online), The Erwin Schrödinger International Institute for Mathematics and Physics (ESI), 11–15 April 2022.
  6. (分岐則の重複度理論と離散的分解: Multiplicities and discrete decomposability for the restriction.) (**6.A.–6.H.** では講演タイトル, 内容は異なるが, 大きなテーマとしては繋がっているので 1 つにまとめる.) **6.A.** Remarks on Branching Laws for  $L^2$ -induced Representations—General Framework. Workshop on “Actions of Reductive Groups and Global Analysis”. Tambara Institute of Mathematical Sciences, 30 Aug 2025. **6.B.** Restricting Representations of Real Reductive Groups to Reductive Subgroups. Séminaire Groupes Réductifs et Formes Automorphes. Institut de Mathématiques de Jussieu-Paris Rive Gauche, France, 17 March 2025. **6.C.** Branching in Representation Theory. Minicourses: branching problems and symmetry-breaking. Institut Henri Poincaré, France, 13–17 January 2025. (three lectures). **6.D.** Branching in Representation Theory. Minicourses: branching problems and symmetry-breaking. Institut Henri Poincaré, France, 13–17 January 2025. (three lectures). **6.E.** Harish-Chandra’s admissibility theorem and beyond. 18th Discussion Meeting in Harmonic Analysis (In honour of centenary

- year of Harish Chandra). IIT Guwahati, India, 18–21 December 2023. **6.F.** Harish-Chandra’s admissibility theorem and beyond. Harish-Chandra Centenary Celebrations 2023: Conference on Harish-Chandra. Harish-Chandra Research Institute (HRI) in Allahabad, India, 9–14 October 2023. **6.G.** Representations and Characters: Revisiting the Works of Harish-Chandra and André Weil — A satellite conference of the virtual ICM 2022 (organized by Hung Yean Loke, Tomasz Przebinda, Angela Pasquale, and Binyong Sun). the Institute for Mathematical Sciences, National University of Singapore, Singapore, 9 July 2022. **6.H.** Bounded multiplicity in the branching problems of “small” infinite-dimensional representations, 5 October 2021. リー群論・表現論セミナー (オンライン), 東京大学.
7. (固有な作用・不連続群と表現論: Proper Actions and Representation Theory.) (**7.A.**–**7.J.** では講演タイトル, 内容は個々に異なるが, 大きなテーマとしては繋がっているので 1 つにまとめる.) **7.A.** Zariski dense subgroups with continuous parameters. Workshop on “Actions of Reductive Groups and Global Analysis”. Tambara Institute of Mathematical Sciences, 27 Aug 2025. **7.B.** Local to Global in Non-Riemannian Geometry, **7.C.** Properness Criterion and its Quantification, **7.D.** Global Analysis on Locally Symmetric Spaces Beyond the Riemannian Case (**7.B.**, **7.C.**, **7.D.** は 2024 年 1 月 1 日 ~3 日に行った Global Analysis of Locally Symmetric Spaces with Indefinite-metric というテーマの 3 回の連続講演. Zariski Dense Subgroups, Number Theory and Geometric Applications. ICTS, Bangalore, India, 1–12 January 2024.) **7.E.** Properness criterion. **7.F.** Discontinuous group, Weil’s local rigidity, and deformation. **7.G.** Tempered Subgroups and tempered homogeneous spaces. (**7.E.**, **7.F.**, **7.G.** は Representations and Characters: Revisiting the Works of Harish-Chandra and André Weil — A satellite conference of the virtual ICM 2022 の 4 連続講演のうちの 3 つ. The Institute for Mathematical Sciences, National University of Singapore, Singapore, 1–15 July 2022. organized by Hung Yean Loke, Tomasz Przebinda, Angela Pasquale, and Binyong Sun). **7.H.** Discontinuous dual and properness criterion (25 April, 2022) **7.I.** The Mackey analogy and proper actions (2 May, 2022) (**7.H.**, **7.I.** は Proper Actions and Representation Theory. Mini-courses of Mini-lectures (Organizers: Pierre Clare, Nigel Higson and Birgit Speh) における 4 つのテーマの講演の 2 つ, AIM Research Community: Representation Theory & Noncommutative Geometry, online), 25 April–16 May 2022. **7.J.** A Program for Branching Problems in the Representation Theory of Real Reductive Groups: Classification Problem of Symmetry Breaking Operators. Representation Theory inspired by the Langlands Conjectures, in connection with the AMS-AWM Noether lecture by Birgit Speh. Denver, USA, 17 January 2020.
8. (緩増加空間の理論: Tempered Homogeneous Spaces.) (**8.A.**–**8.S.** では講演タイトル, 内容は個々に異なるが, 大きなテーマとしては繋がっているので 1 つにまとめる.) **8.A.** Basic Questions in Group Theoretic Analysis on Manifolds II, Analytic Representation Theory in Tokyo. École thématique du CNRS ARTinTOKYO, Tokyo, Japan, 4–8 Nov. 2025. **8.B.** Tempered Homogeneous Spaces. Symposium on Representation Theory 2025. IT Extension Center, Kanagawa Institute of Technology, Atsugi, Kanagawa, Japan, 24–26 Nov. 2025. **8.C.** Structure of Tempered Homogeneous Spaces. III. Limit Algebras. Mini-courses. Institut Henri Poincaré, France,

21 February 2025. (Day 3 of the three lectures). **8.D.** Structure of Tempered Homogeneous Spaces. II. Combinatorics Approach. Minicourses. Institut Henri Poincaré, France, 19 February 2025. (Day 2 of the three lectures). **8.E.** Structure of Tempered Homogeneous Spaces. I. Dynamical Approach. Minicourses. Institut Henri Poincaré, France, 17 February 2025. (Day 1 of the three lectures). **8.F.** Structure of Tempered Homogeneous Spaces. III. Limit Algebras. Minicourses. Institut Henri Poincaré, France, 21 February 2025. (Day 3 of the three lectures). **8.G.** Structure of Tempered Homogeneous Spaces. II. Combinatorics Approach. Minicourses. Institut Henri Poincaré, France, 19 February 2025. (Day 2 of the three lectures). **8.H.** Structure of Tempered Homogeneous Spaces. I. Dynamical Approach. Minicourses. Institut Henri Poincaré, France, 17 February 2025. (Day 1 of the three lectures). **8.I.** Tempered homogeneous spaces and tempered subgroups — Dynamical approach **8.J.** Classification theory of non-tempered  $G/H$  — Combinatorics of convex polyhedra **8.K.** Tempered homogeneous spaces — Interaction with topology and geometry (**8.I.**, **8.J.**, **8.K.** は Harish-Chandra’s Tempered Representations and Geometry. 18th Discussion Meeting in Harmonic Analysis (In honour of centenary year of Harish-Chandra): Workshop. IIT Guwahati, India, 12-16 December 2023 における 4 連続講演のうち 3 つ) **8.L.** Tempered subgroups à la Margulis (9 May, 2022). **8.M.** Tempered homogeneous spaces (16 May 2022) (**8.L.**, **8.M.** は Proper Actions and Representation Theory. Mini-courses of Mini-lectures (Organizers: Pierre Clare, Nigel Higson and Birgit Speh) における 4 連続講演のうち 2 つ, AIM Research Community: Representa-

tion Theory & Noncommutative Geometry, online), 25 April-16 May 2022. **8.N.** Symmetry in Geometry and Analysis, In honour of Professor Toshiyuki Kobayashi (organized by M. Pevzner and H. Sekiguchi). Reims University, France, 6–10 June 2022. **8.O.** 緩増加な等質空間 (Tempered Homogeneous Spaces). 日本数学会年会函数解析学分会特別講演 (慶応大学, オンライン), 16 March 2021. **8.P.** Limit Algebras and Tempered Representations. (opening lecture). RIMS Workshop: Lie Theory, Representation Theory and Related Areas. (online), 10 August 2021. **8.Q.** Limit Algebras and Tempered Representations. (plenary opening lecture). XIV. International Workshop: Lie Theory and Its Applications in Physics. Bulgaria (online), 20–26 June 2021. **8.R.** Limit algebras and tempered representation. Lie Groups and Representation Theory Seminar. The University of Tokyo, 15 June 2021. **8.S.** This is What I do: Limit algebras and tempered representations. Representation Theory & Noncommutative Geometry. AIM Research Community (online), 8 April 2021.

9. (等質空間上の大域解析・実球等質空間の一般理論: Regular Representations on Homogeneous Spaces.) (**9.A.**–**9.L.** では講演タイトル, 内容は個々に異なるが, 大きなテーマとしては繋がっているので 1 つにまとめる.) **9.A.** Basic Questions in Group-Theoretic Analysis on Manifolds. I. Analytic Representation Theory in Tokyo. École thématique du CNRS ARTinTOKYO, Tokyo, Japan, 4–8 Nov 2025. **9.B.** Basic Questions in Group-Theoretic Analysis on Manifolds. Introductory school at CIRM (Marseille): Methods in representation theory and operator algebras. Marseille, France, 6-10 January 2025. **9.C.** Basic Questions in Group-Theoretic Analysis on Manifolds. Introductory school at CIRM (Marseille): Methods in representation theory

- and operator algebras. Marseille, France, 6–10 January 2025. **9.D.** Basic Questions in Group-Theoretic Analysis on Manifolds. Colloquium at Hiroshima University. Hiroshima, Japan, 22 October 2024. **9.E.** Overview of Branching Problems in the Real Setting. Branching Problems for Representations of Real,  $p$ -Adic and Adelic Groups. the University of British Columbia - Okanagan, Kelowna, Canada. BIRS, 7–12 July 2024. **9.F.** Is representation theory useful for global analysis on a manifold? — Multiplicity: Approach from PDEs, Harish-Chandra’s Tempered Representations and Geometry IIT Guwahati, India, 12-16 December 2023. (Harish-Chandra 生誕 100 年を記念した 4 回の連続講義の第 1 回目) **9.G.** Is representation theory useful for global analysis on a manifold? — Multiplicity: Approach from PDEs, **9.H.** Tempered homogeneous spaces and tempered subgroups — Dynamical approach, **9.I.** Classification theory of non-tempered  $G/H$  — Combinatorics of convex polyhedra, **9.J.** Tempered homogeneous spaces — Interaction with topology and geometry, (**9.G.**, **9.H.**, **9.I.**, **9.J.** は Analysis on Homogeneous Spaces における 4 回連続講演, Noncommutative Geometry and Analysis on Homogeneous Spaces. Williamsburg, USA, 16–20 January 2023.) **9.K.** Basic Questions in Group-Theoretic Analysis on Manifolds. MATH-IMS Joint Pure Mathematics Colloquium Series. The Chinese University of Hong Kong, 25 November 2022. **9.L.** A Foundation of Group-theoretic Analysis on Manifolds. Colloquium di dipartimento. Dipartimento di Matematica, Università di Roma “Tor Vergata” (online), 18 February 2021.
10. (擬リーマン対称空間におけるスペクトル解析: Global Geometry and Analysis on Locally Symmetric Spaces—Beyond the Riemannian Case.) (**10.A.–10.H.** では講演タイトル, 内容は個々に異なるが, 大きなテーマとしては繋がっているので 1 つにまとめる.) **10.A.** Spectral Analysis on Locally Symmetric Spaces Beyond the Riemannian Setting: Hidden Symmetries and Representation Theory. Séminaire Orléans. Institut Denis Poisson, Orleans, France, 11 Sep 2025. Rescheduled to 18 Sept due to the general strike. **10.B.** Spectral Analysis on Standard Locally Homogeneous Spaces—Application of Branching Problems arising from Proper Actions. Workshop on “Actions of Reductive Groups and Global Analysis”. Tambara Institute of Mathematical Sciences, 31 Aug 2025. **10.C.** Hidden Symmetry and Spectral Analysis on Locally Pseudo-Riemannian Symmetry Spaces. Intertwining Operators and Geometry during the thematic trimester Representation Theory and Noncommutative Geometry. Institut Henri Poincaré, France, 20–24 January 2025. **10.D.** Hidden Symmetry and Spectral Analysis on Locally Pseudo-Riemannian Symmetry Spaces. Intertwining Operators and Geometry during the thematic trimester Representation Theory and Noncommutative Geometry. Institut Henri Poincaré, France, 20–24 January 2025. **10.E.** Branching Problems and Global Analysis of Locally Symmetric Spaces with Indefinite-Metric. Seminar at University of Trento. Trento, Italy, 19 September 2024. **10.F.** Branching Problems and Global Analysis of Locally Symmetric Spaces with Indefinite-Metric. International Congress of Basic Science. Beijing, China, 25 July 2024. **10.G.** Global Analysis of Locally Symmetric Spaces with Indefinite-metric. Colloquium, National University of Singapore. (online), 13 August 2021. **10.H.** Sound of an anti-de Sitter manifold. (opening lecture). Inaugu-

ral Day of the French–Kazakhstan school of Mathematics. (online), 25 June 2021.

D. 講義

1. 数理科学概論 I (文科生) (教養学部文科 1,2 年生, 2025 年度 A セメスター, 対面): フェルミ推定, 微積分, Taylor 展開, 偏微分, Lagrange の未定乗数法, 近似と概算, 微分方程式の初歩, 多変数関数の積分を講義した.
2. 基礎数理特別講義 VIII/幾何学 XH (数理大学院・4 年生共通講義, 2025 年度 A セメスター, 対面): 解析的表現論. 複素多様体およびその変換群に関する基礎的な事項を説明し, その後, 確定特異点型微分方程式の境界値問題を概説した. さらに, 2 つの同変ベクトル束を舞台として非局所的な対称性破れ作用素や絡作用素の構成の一般論を紹介した. これらを融合する形でユニタリ表現の行列要素の漸近挙動の関係を Poisson 変換や Knapp–Stein 作用素について解説した. 最後に, ユニタリ表現を用いた不連続群論への応用として, Margulis による measurably proper actions の理論とその応用を概説した.
3. (フランスでの連続講義 1 : 対称性の破れ作用素の理論) Branching in Representation Theory. Minicourses: branching problems and symmetry-breaking. Institut Henri Poincaré, France, January 2025.

The concept of symmetries naturally arises in various areas of mathematics and science, including geometry, number theory, differential equations, and quantum mechanics. The more symmetries an object possesses, the better we can understand it through group-theoretic approaches.

Branching problems investigate how large symmetries break down into smaller ones, such as fusion rules, using mathematical formulations based on the language of representations and their restrictions. These problems have been studied for over 80 years. In recent years, there has been a surge of research focused on the restriction of continuous symmetries in infinite-

dimensional cases, leading to the development of new geometric and analytic methods.

I provided an introduction to the branching problems of infinite-dimensional representations of real reductive groups, such as  $GL(n, \mathbb{R})$ , using plenty of elementary examples to make the basic concepts and key ideas more accessible.

4. (フランスでの連続講義 2 : 緩増加空間の理論) Structure of Tempered Homogeneous Spaces Institut Henri Poincaré, France, February 2025.

The lectures introduce recent theories of tempered spaces, and I plan to provide an overview of these topics, using plenty of elementary examples to make the basic concepts and key ideas more accessible.

1. I will review basic concepts such as tempered unitary representations of real reductive groups, like  $GL(n, \mathbb{R})$ , as well as “tempered” spaces and “tempered subgroups”. I will begin with some geometric observations of group actions, including the properness criterion for reductive homogeneous spaces. Subsequently, I will introduce a “quantification” of proper actions and incorporate a dynamical approach into analytic representation theory, including the temperedness criterion for homogeneous spaces, which was developed recently by Y. Benoist and the speaker, drawing on the Cowling-Haagerup-Howe theory and other related ideas.

2. The criterion for tempered spaces, explained in the first lecture, is computable. In this lecture, I will explain how this criterion leads to the classification theory of non-tempered reductive homogeneous spaces by breaking it down into several steps. The technical methods used in the second lecture differ from the dynamical approach presented in the first lecture. Our approach relies on elementary

results from finite-dimensional representations and some combinatorics of convex polyhedral cones.

3. Recently, surprising and intriguing connections have been observed between the concept of “tempered spaces for unitary representations” and various other areas of mathematics. In this lecture, we will explore different aspects of tempered spaces from the perspectives of topology and geometry, including limit algebras (collapsing Lie algebras) and geometric quantization.
5. 数学講究 XA (数学科 4 年生, 2025 年度 S セメスター, 対面): 2 つのテキスト, Wells 著, Differential Analysis on Complex Manifolds (GTM), および, Duistermaat–Kolk 著, Lie Groups (Universitext), Springer によるセミナーを行った。
6. 数学特別講究 (数学科 4 年生, 2025 年度 A セメスター, 対面): 2 つのテキスト, Wells 著, Differential Analysis on Complex Manifolds (GTM), および, Duistermaat–Kolk 著, Lie Groups (Universitext), Springer によるセミナーを行った。
7. 数学講究 XB (数理科学概論)「対称性の数学」, (理学部数学科 4 年生), 2025 年 5 月 7 日。

#### E. 修士・博士論文

1. (博士) 樋川達郎 (HIKAWA Tatsuro): On the  $(k, a)$ -generalized Fourier transform and the minimal representation of the conformal group, (和訳:  $(k, a)$  一般化 Fourier 変換と共形変換群の極小表現について), 2026 年 3 月。

#### F. 対外研究サービス

1. 日仏数学連携拠点 FJ-LMI (French-Japanese Laboratory of Mathematics and its Interactions), 日本側拠点長 (co-director) (2023 年 9 月 1 日–)。
2. Kavli IPMU(数物宇宙連携機構), 上席科学研究員併任 (2009.8–2011.5); 主任研究員 (Principal Investigator) 併任 (2011.6–2022.3); 客員上級科学研究員併任 (2022.4–);

シニアフェロー併任 (2025.4–)。

[ジャーナルのエディター]

3. Editor in Chief, Japanese Journal of Mathematics (日本数学会, Springer-Nature) (2006–)
  4. Editor, International Mathematics Research Notices (Oxford 大学出版) (2002–2021)
  5. Editor in Chief, Takagi Booklet, vol. 1–22 (日本数学会) (2006–)
  6. Editor, Geometriae Dedicata (Springer) (2000–)
  7. Editor, Advances in Pure and Applied Mathematics (de Gruyter) (2008–)
  8. Editor, International Journal of Mathematics (World Scientific) (2004–)
  9. Editor, Journal of Mathematical Sciences, The University of Tokyo (2007–)
  10. Editor, Kyoto Journal of Mathematics (2010–)
  11. Editor, Representation Theory (アメリカ数学会) (2015–2019)
  12. Editor, AMS Translation Series (アメリカ数学会) (2016–)
  13. Editor, Tunisian Journal of Mathematics (2017–)
  14. Editor, Special Issue in commemoration of Professor Kunihiko Kodaira’s centennial birthday (J. Math. Sciences, The University of Tokyo).
  15. Editor, Special Issue in honor of Professor Masaki Kashiwara’s 70th birthday (Publ. RIMS) 2017–2021.
  16. Chief Editor, Mikio Sato’s Collected Papers, (Springer-Nature).
  17. 共立出版, 『共立講座 数学探検 (全 18 巻)』, 『共立講座 数学の魅力 (全 14 巻 + 別巻 1)』, 『共立講座 数学の輝き (全 40 巻予定)』の 3 シリーズ編集委員
  18. 編集委員, 『数学の現在  $i, e, \pi$ 』, および続刊 『数学の現在  $\pi \times i, e + \pi$ 』, (with 斎藤毅, 河東泰之), 東京大学出版会 2016; 2025.
- [学会・他大学の委員など]
19. ICM2022 における招待講演者および Ple-

- inary lecturers の選考に関する国際委員会の議長 (Chair, Lie Theory and its generalizations, ICM2022), 2019–2022.
20. 国際賞 (Shaw Prize) の授賞委員会: Committee of Shaw Prize, 2020–2021, 国外.
  21. 国際賞 (Shaw Prize) の授賞委員会: Committee of Shaw Prize, 2019 および 2020, 国外.
  22. 国際数学者賞の授賞委員会: Prize Committee (International Prize, 数学部門) 2018, 国外.
  23. ICM2030 招致 招致委員 (2025–).
  24. 国内の数学の賞 (複数) の授賞委員会 (anonymous, various years).
  25. 京都大学数理解析研究所運営委員 (2015–2017; 2017–2019).
  26. 京都大学数理解析研究所専門委員 (2007–2009; 2009–2011; 2015–2017; 2017–2019; 2021–2023; 2025–).
  27. 科学研究費等の審査委員: 日本 (JSPS), 米国 (NSF-AMS), EU, ドイツ, ルクセンブルク, 中華人民共和国・香港 (various years).
  28. OIST (沖縄科学技術大学大学院) の数学部門に対する国際 Advisory Board Member (2021–2023).
  29. 東京大学数学同窓会副理事長 (2026–).  
[国際研究集会のオーガナイザーなど]
  30. オーガナイザー, 日仏数学連携拠点: 解析的表現論スクール/ CNRS Thematic School in Tokyo Analytic Representation Theory. November 4–8, 2025.
  31. Scientific Committee, “Representation Theory and Non Commutative Geometry” at IHP 2025, Paris, France.
  32. オーガナイザー, Summer School on Representation theory, リー群の群作用と大域解析に関するセミナー, 玉原国際セミナーハウス, 27–31 August 2025.
  33. オーガナイザー, 日仏数学連携拠点開設記念コンファランス (Opening Conference of French-Japanese Laboratory of Mathematics and its Interactions), April 4–5, 2024 (with M. Pevzner).
  34. オーガナイザー, Periods and Branching Problems for Representations of Real,  $p$ -adic and Adelic Groups, BIRS Conference, Canada, July 2024 (with M. Pevzner, B. Speh).
  35. オーガナイザー, Summer School on Representation Theory, リー群の群作用と大域解析に関するセミナー, (Virtual 玉原国際セミナーハウス), 19–23 August 2024.
  36. オーガナイザー, Summer School on Representation Theory, リー群の群作用と大域解析に関するセミナー, (virtual 玉原国際セミナーハウス), August 19–23, 2023 (オンライン).
  37. オーガナイザー, Summer School on Representation Theory, リー群の群作用と大域解析に関するセミナー, (virtual 玉原国際セミナーハウス), August 17–21, 2022 (オンライン).
  38. オーガナイザー, Summer School on Representation Theory, リー群の群作用と大域解析に関するセミナー, (virtual 玉原国際セミナーハウス), August 17–21, 2021(オンライン).
  39. オーガナイザー, Integral Geometry, Representation Theory and Complex Analysis, Kavli Institute for the Physics and Mathematics of the Universe, 27–28 January 2020.
  40. オーガナイザー, 高木レクチャー, 創設責任者. オーガナイザー第1回-第24回 (currently with Y. Kawahigashi, T. Kumagai, H. Nakajima, K. Ono and T. Saito).
  41. オーガナイザー, リー群論・表現論セミナー (2007–present 東大; 2003–2007 RIMS; 1987–2001 東大)
  42. オーガナイザー, 日仏数学連携拠点, FJ-LMI コロキウム, 2023.10– (with M. Pevzner).  
[アウトリーチ]
  43. 群馬県立太田高等学校の大学訪問, 模擬講義, 2023年11月8日.
  44. (インタビュー) Interview of Toshiyuki Kobayashi by Chee Whye Chin, IMPRINTS, 2024, Newsletter of the Institute of Mathematical Sciences, Natural Univer-

sity of Singapore, pp. 19–29.

#### G. 受賞・栄誉

1. W. M. Goldman et al, The Mathematical Work of Toshiyuki Kobayashi, Symmetry in Geometry and Analysis, Volume 1, Progress in Mathematics **357** (2025), Springer-Nature, pages 1-102.
2. Doctorat Honoris Causa (University of Reims), 2022, France.
3. 日本数学会出版賞 (2019) 『数学の現在  $i, e, \pi$ 』東京大学出版会, (斎藤毅氏, 河東泰之氏との共同受賞).
4. アメリカ数学会フェロー (2017) 「簡約リー群の構造論と表現論に対する貢献」(Contribution to Structure Theory and Representation Theory of Reductive Lie groups).
5. 紫綬褒章 (Medal with Purple Ribbon)(2014) 「数学研究」.
6. [学生の受賞] 東京大学学位記授与式における総代, Víctor Pérez-Valdés, (2024年3月, 総代),  
東京大学学位記授与式における総代, 甘中一輝 (2021年3月, 総代・答辞),

#### H. 海外からのビジター

1. Michael Pevzner (University of Reims, France), September 2023–, French-Japanese Laboratory of Mathematics and its Interactions, director.
2. Fanny, Kassel (IHES) Giving an invited lecture at the Takagi Lecture. 高木レクチャーにおいて招待講演 “Discrete Subgroups of Lie Groups and Proper Actions”(リー群の離散部分群と固有な作用) を行う (2025, November).
3. Sourav Ghosh (Ashoka University) Anosov 表現を用いた離散群の変換理論の研究を行う。また Proper actions on group manifolds のテーマで講演を行った。(2025, October).
4. Jonathan Ditlevsen, October 2024–2026. He is a postdoc scholar working on symmetry breaking.
5. Paolo Ciatti (Padova University, Italy),

(2025, June). He gave a lecture on “Spectral estimates on the Heisenberg group” in the FJ-LMI colloquium; Valentina Casarino (Università degli Studi di Padova, Italy), (2025, June). She gave a lecture on “Variational inequalities in a nonsymmetric Gaussian framework” in the FJ-LMI colloquium.

#### 連携併任講座