

Synthetic theory of Ricci curvature bounds^{*}

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Abstract. Synthetic theory of Ricci curvature bounds is reviewed, from the conditions which led to its birth, up to some of its latest developments.

Keywords and phrases: Ricci curvature, optimal transport, metric geometry, synthetic geometry, information geometry

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