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A. 研究概要

1.D 型極小表現の幾何・解析的研究

極小表現は、ユニタリ表現の中で根源的な対象であると考えられ、90年代より多くの代数的研究がなされている(古典的な Weil 表現は C 型単純群の極小表現である)。同じ対象を解析的に捉えて新しいモデルを構成することを目指し、[1]では D 型極小表現の共形幾何による新構成を行い、超双曲型微分方程式の解の共形保存量を具体的に構成してユニタリ化の別証明を与え、加えて、Schrödinger モデルの存在を証明した。さらに錐上の L^2 解析において“フーリエ変換”に相当する基本的な作用素であるユニタリ反転変換を群論的に定義し、その形を決定した [4,6,10]。

2. 可視的作用と無重複表現

複素多様体における可視的作用という概念と無重複性の伝播という視点を導入し、無限次元の場合および(組合せ論が絡む)有限次元の場合を同時に含む、無重複表現の統一的な理論をめざしている。論文 [5,8] は可視的作用の分類、[7] は表現論への応用である。

3. 不連続群

私の長年のモチーフである非リーマン空間における不連続群の研究を続けた。特に、変形中に不連続性が破れる様子を調べるために、局所剛性の概念に加えて、安定性の概念を導入した (IJM2006 及び preprint)。また、不定符号の空間形の対称空間における余コンパクトな不連続群が存在するための必要十分条件を決定した [3]。

4. 実解析

Riesz 変換のように対称性の高いマルチプライヤー作用素を全て捕捉する代数的枠組みを与え、その L^p 有界性を研究した [9]。

1. Analysis on minimal representations

Minimal representations are building blocks of unitary representations. Classic examples are the Weil representation, and intensive algebraic studies have been made since 1990s by many people. Aiming for yet another *geometric approach* to minimal representations, in particular of type D , we applied conformal techniques, got a new construction of minimal representations, found conserved quantities for ultra-hyperbolic equations that led us to their unitarizability, and also proved the existence of a

Schrödinger model (L^2 -model) with B.Ørsted [1]. With G. Mano [4,6,10], we determined an explicit form of the *unitary inversion operator* on the L^2 -model on the isotropic cones, that generalizes the Euclidean Fourier transform.

2. Multiplicity-free representations

I made in [7] systematic and synthetic applications of the original theory of *visible actions* on complex manifolds to multiplicity-free theorems, in particular, branching problems to symmetric pairs. Papers [5,8] are on visible actions.

3. Discontinuous groups Developing my conituing motif on discontinuous groups for non-Riemannian homogeneous spaces, I introduced the notion of *stability* for the study of *local deformation/rigidity* of discontinuous groups [IJM2006], and determined when the tangential space forms of general signature admits compact forms by means of the Radon-Hurwicz number with Yoshino [3].

4. Real analysis - L^p multipliers

Inspired by the idea of prehomogeneous spaces, we studied multipliers with high symmetries with Nilsson [9].

B. 発表論文

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C. 口頭発表

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D. 講義

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E. 修士・博士論文

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F. 対外研究サービス

1. Managing Editor, Japanese Journal of Mathematics (日本数学会) (2005-)

2. Editor, Geometriae Dedicata (Springer) (2000-)
3. Editor, International Mathematics Research Notices (Oxford 大学出版) (2002-)
4. Editor, International Journal of Mathematics (World Scientific) (2004-)
5. Editor, International Mathematics Research Papers (Oxford 大学出版) (2005-)
6. Editor, Journal of Mathematical Sciences, The University of Tokyo (2007-)
7. Editor, Advances in Pure and Applied Mathematics (Heldermann Verlag) (2008-)
8. Editor in Chief, Journal of Mathematical Society of Japan (日本数学会) (2002-2004; 2004-2006), Editor (1998-2006)
9. Editor, Publications RIMS (2003-2007)
10. 日本学術会議連携会員 (2006-)
11. 日本数学会評議員 (2003-2005; 2005-2007)
12. 日本数学会理事 (2003-2005; 2005-2007)
13. 京都大学数理解析研究所専門委員 (2007-)
14. Jury, Habilitation, Reims University, France (2006)
15. オーガナイザー, Symposium on Representation Theory, 淡路島, 2004 年 11 月 16-19 日 (with H. Ochiai and H. Tagawa)
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G. 受賞

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3. Sackler Distinguished Lecturer (2007)

H. 海外からのビジター

1. Professor Dr. Pablo Ramacher (2007 Fall)
2. Professor Misha Pevzner (2007–2008.1), JSPS fellow
3. Professor Salma Nasrin (2007.12)
4. Professor Dr. Karl-Hermann Neeb (2007.5)
5. Professor Dr. Martin Olbrich (2007.9)