Lie Groups and Representation Theory Seminar at the University of Tokyo

リー群論・表現論セミナー

SPEAKER Benjamin Harris (Louisiana State University, USA)

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PLACE Room 126, Graduate School of Mathematical Sciences

TITLE Representation Theory and Microlocal Analysis

ABSTRACT Suppose $H \subset K$ are compact, connected Lie groups, and suppose τ is an irreducible, unitary representation of H. In 1979, Kashiwara and Vergne proved a simple asymptotic formula for the decomposition of $\operatorname{Ind}_{H}^{K} \tau$ by microlocally studying the regularity of vectors in this representation, thought of as vector valued functions on K. In 1998, Kobayashi proved a powerful criterion for the discrete decomposability of an irreducible, unitary representation π of a reductive Lie group G when restricted to a reductive subgroup H. One of his key ideas was to restrict π to a representation of a maximal compact subgroup $K \subset G$, view π as a subrepresentation of $L^2(K)$, and then use ideas similar to those developed by Kashiwara and Vergne.

In a recent preprint the speaker wrote with Hongyu He and Gestur Olafsson, the authors consider the possibility of studying induction and restriction to a reductive Lie group G by microlocally studying the regularity of the matrix coefficients of (possibly reducible) unitary representations of G, viewed as continuous functions on the (possibly noncompact) Lie group G. In this talk, we will outline the main results of this paper and give additional conjectures.