Lie Group and Representation Theory Seminar

Date:	February 10 (Tue), 2004, 17:00–18:00
Place:	RIMS 402
Speaker:	Soo Teck Lee (NUS, Singapore)
Title:	A basis for the k-fold tensor product algebra of $\operatorname{GL}_n(\mathbb{C})$

Abstract:

In this talk, I will disucss the recent work of Howe-Tan-Willenbring and Howe-Lee.

For each positive integer m, let U_m denote the maximal unipotent subgroup of $\operatorname{GL}_m(\mathbb{C})$ consisting of all upper triangular matrices with 1 on the diagonal. Let $l_1, \ldots, l_k \leq n$ and $l = l_1 + \cdots + l_k$. Let the group $\operatorname{GL}_n(\mathbb{C}) \times \operatorname{GL}_{l_1}(\mathbb{C}) \times \cdots \times \operatorname{GL}_{l_k}(\mathbb{C})$ act on

$$M_{nl}(\mathbb{C}) \cong M_{n,l_1}(\mathbb{C}) \oplus \cdots \oplus M_{n,l_k}(\mathbb{C})$$

by

$$(g, h_1, ..., h_k).(T_1, ..., T_k) = \left((g^{-1})^t T_1 h_1^{-1}, ..., (g^{-1})^t T_k h_k^{-1} \right)$$

where $g \in \operatorname{GL}_n(\mathbb{C})$, $h_i \in \operatorname{GL}_{l_i}(\mathbb{C})$ and $T_i \in \operatorname{M}_{n,l_i}(\mathbb{C})$ for $1 \leq i \leq k$. This action induces an action on the algebra $\mathcal{P}(\operatorname{M}_{nl})$ of polynomial functions on $\operatorname{M}_{nl}(\mathbb{C})$. The algebra

$$\mathcal{P}(\mathbf{M}_{nl})^{U_n \times U_{l_1} \times \cdots \times U_{l_k}}$$

of $U_n \times U_{l_1} \times \cdots \times U_{l_k}$ invariants contains information on the decomposition of k-fold tensor products of finite dimensional irreducible representations of $\operatorname{GL}_n(\mathbb{C})$. So it is called a k-fold tensor product algebra of $\operatorname{GL}_n(\mathbb{C})$. In this talk, we shall construct a basis for this algebra.

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