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Generic singularities of implicit systems of first order differential equations on the plane

A.A. Davydov[*] · G. Ishikawa[**] · S. Izumiya[***] · W.-Z. Sun[†]

Abstract. For the implicit systems of first order ordinary differential equations on the plane there is presented the complete local classification of generic singularities of family of its phase curves up to smooth orbital equivalence. Besides the well-known singularities of generic vector fields on the plane and the singularities described by a generic first order implicit differential equations, there exists only one generic singularity described by the implicit first order equation supplied by Whitney umbrella surface generically embedded to the space of directions on the plane.

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A.A. DAVYDOV
Department of Mathematics, Vladimir State University, Gorkii street 87, 600026 Vladimir, Russia
(e-mail: davydov@vpti.vladimir.ru)
G. ISHIKAWA
Department of Mathematics, Hokkaido University, Sapporo 060-0810, Japan
(e-mail: ishikawa@math.sci.hokudai.ac.jp)
S. IZUMIYA
Department of Mathematics, Hokkaido University, Sapporo 060-0810, Japan
(e-mail: izumiya@math.sci.hokudai.ac.jp)
W.-Z. SUN
School of Science, Changchun University of Science and Technology, Changchun 130022, China
(e-mail: wzsun@cust.edu.cn)