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#### A. 研究概要

前年度の、等標数の局所体の分岐群の研究に引きつづき、混標数の場合の研究を進めた。離散付値環の長さ有限な商環について、分岐群の関手性を示すことにより、等標数の場合と同様に、分岐群の部分商の可換性およびその指標群の記述を示すことができた。

Following the success on the study of the ramification groups of the local fields of equal characteristic in the last year, I studied the mixed characteristic case. By establishing the functoriality of the ramification groups for truncated discrete valuation rings, I proved the commutativity and a description of the character group of a graded quotient of the ramification groups, similarly as in the equal characteristic case.

#### B. 発表論文

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#### F. 対外研究サービス

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